Time-varying effects of search engine advertising on sales—An empirical investigation in E-commerce

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ARTICLE INFO

Keywords:
Online advertising
Electronic commerce
Advertising analytics
Business intelligence

ABSTRACT

As a mainstream advertising channel, Search Engine Advertising (SEA) has a huge business impact and attracts a plethora of attention from both academia and industry. One important goal of SEA is to increase sales. Nevertheless, while previous research has studied multiple factors that are potentially related to the outcome of SEA campaigns, effects of these factors on actual sales generated by SEA remain understudied. It is also unclear whether and how such effects change over time in dynamic SEA campaigns that last for an extended period of time. As the first empirical investigation of the dynamic advertisement-sales relationship in SEA, this study builds an advertising response model within a time-varying coefficient (TVC) modeling framework, and estimates the model using a unique dataset from a large e-commerce retailer in the United States. Results reveal the effects of the advertising expenditure, consumer behaviors and advertisement characteristics on realized sales, and demonstrate that such effects on sales do change over time in non-linear ways. More importantly, we find that carryover has a stronger effect in generating sales than immediate or direct response does, and advertisers need to carefully decide how much to bid for higher ad positions. These findings have direct implications for business decision-making to launch more effective SEA campaigns and for SEA platforms to improve their pricing mechanism.

1. Introduction

During the past decade, search engine advertising (SEA) has become one of the most prominent outlets for online advertising campaigns. Through SEA, advertisers pay search engines to display their advertisements related to search queries along with organic results on search engine result pages (SERPs). The economic impact of SEA has been well documented. According to the Interactive Advertising Bureau (2018), SEA revenue in the U.S. alone exceeded 22 billions USD during the first half of 2018, accounting for nearly half of the total revenue for online advertising during that period. With the high expenditure on SEA, advertisers are eager to know what drives the outcome of SEA campaigns. Although SEA success can be measured in different ways (e.g., online traffic and brand awareness), sales are typically one of the most important criteria advertisers care about, especially in e-commerce [1]. Indeed, a better understanding of the ad-sales relationship can help advertisers make more effective investment decisions in SEA campaigns and aid SEA platforms in advertising mechanism design.

SEA is a much more dynamic and evolving market [2] than traditional marketing channels (e.g., newspapers and TV). At the core of SEA is real-time position auctions run by search engines to determine which ads to be displayed on a SERP and their rankings. As participants of these auctions, advertisers need to make decisions on expenditures by considering a range of factors related to consumer behaviors (e.g., ad clicks and product purchases), characteristics of advertisement (e.g., keywords and ad positions) as well as competitions from other advertisers. Note that the values of these factors to advertisers could change over time [3,4]. As a result, it has been well-recognized by advertisers that strategies governing SEA campaigns need to be dynamically adjusted in order to achieve more sales [5,6,7,8,9,10].

Although business needs of understanding dynamic ad-sale relationships in SEA are clear, very little research has investigated the drivers of sales volume generated from SEA. Previous studies of SEA have mainly investigated measures related to consumers’ clicks on ads

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https://doi.org/10.1016/j.dss.2022.113843
Received 10 January 2022; Received in revised form 15 July 2022; Accepted 16 July 2022
Available online 23 July 2022
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Please cite this article as: Yanwu Yang, Decision Support Systems, https://doi.org/10.1016/j.dss.2022.113843
and conversions. While intuitive and easy to obtain, clicks on ads and conversions are not equal to sales. Even customers who clicked the same ad may purchase the advertised product in different quantities, leading to different amounts of sales. Although earlier studies have attempted to associate the advertising expenditure with sales [11] and quantify the relative effectiveness across different channels [12], these models did not consider other important factors beyond the expenditure, and analyze the ad-sales relationship in a static way.

Therefore, a critical gap exists for researchers to investigate the effects of a comprehensive set of factors on sales from SEA over time. For example, SEA has been commonly recognized as a form of direct response advertising and a short-term investment [13], such that e-commerce firms pay to attract traffic to their own websites and advertised product pages, which may generate online transactions immediately. Many advertisers believe such effects will stop after the expenditure on SEA campaigns stops. However, while researchers have questioned this conventional belief [14,15,16], there lacks a formal study on whether the effectiveness of SEA occurs in a direct (i.e., immediate), or indirect (i.e., time-lagged) manner. Besides the expenditure, other factors related to consumer behaviors (e.g., click-through rate (CTR), conversion rate (CVR), cost-per-click (CPC)), and advertisement characteristics (e.g., keywords and ad positions in SERPs) could also affect sales. Nevertheless, no studies have directly compared their effects with each other or analyzed how their effects change over time.

To address the aforementioned gap and challenges, this paper represents the first effort to empirically explore the dynamic advertising-sales relationship in SEA. Specifically, this research builds an advertising response model within a time-varying coefficient (TVC) modeling framework [17] to capture the dynamic nature of SEA markets. We choose the partial adjustment model [18,19] to examine the carryover effect in SEA. We empirically estimate our response model using a unique panel dataset collected from SEA campaigns by a large U.S. e-commerce retailer.

The contributions of our study and how the paper can support decision-making can be summarized as follows.

First, we are the first study to empirically reveal the dynamic nature of SEA—the effects of various factors on SEA sales do change over time. Our work offers a new perspective compared to previous studies that mainly focus on the overall static effects of different factors. Such dynamics in SEA have important implications for advertisers—they must continuously track and predict the real-time effectiveness of their SEA campaigns, so that they can make better decisions and adjust their advertising strategies. Moreover, the changing pattern of advertising factors over time differs, which may offer valuable insights for advertisers’ decision-making and planning.

Second, one surprising finding by adopting a dynamic perspective is that the ad-sales relationship in SEA demonstrates a strong carryover effect. This contradicts the commonly held view that SEA is a direct-response advertising medium that mainly generates immediate or direct effects (e.g., sales) [20,21,22]. Instead, SEA advertisers may need to be more patient, and their decisions have to be based on longer-term efforts. Meanwhile, without considering the carryover effect, the immediate effect of the advertising expenditure on sales may be either underestimated (for newly launched advertisements) or overestimated (for advertisements that have been delivered for a long time) and could lead to inefficient spending decisions.

Last, this research suggests that advertisers need to pay extra attention to ad positions. While a higher position is associated with more sales, advertisers’ costs to bid for better positions may not be covered by the consequent gains in sales, especially when the positive effect of ad positions decays quickly over time. In other words, contrary to the typical SEA strategy of always bidding for the highest ad position on SERPs as previous studies suggested [23,24], we encourage advertisers to base their bidding decisions on expected future sales gains over time.

A better understanding of the dynamic ad-sales relationship in SEA has tremendous values. Because spending more in SEA does not necessarily lead to higher sales [25,8], advertisers need to make their budget allocation taking into account advertising dynamics in SEA to maximize their returns in the ever-changing market. Such real-time decision support in SEA is especially important for advertisers from small and medium enterprises, who represent the main revenue sources for search engines but have limited resources to understand such complexity and optimize budgets for their SEA campaigns [26].

The remainder of this paper is organized as follows. Section 2 presents a brief survey of related research. This is followed by descriptions of our data and key variables used in this research in Section 3. In Section 4, we discuss basic principles of the time-varying modeling framework and present a time-varying response model for SEA. Empirical results are listed in Section 5. The last section concludes with managerial implications and theoretical contributions, and future research directions.

2. Related literature and theoretical background

This paper studies the dynamic ad-sales relationship in SEA and is related to literature from three streams of research: (i) factors related to the performance of SEA campaigns, (ii) dynamic processes and advertising decisions in SEA, and (iii) time-varying modeling.

The growth of SEA has motivated studies that investigated factors for the success of SEA campaigns. An advertiser’s expenditure is critical for its SEA campaigns to gain more visibility and revenue [27,28]. The advertising expenditure affects sales in two possible ways: (1) Direct via immediate response (a.k.a., short-term advertising elasticity)—the current advertising expenditure affects current sales directly and immediately [29,30]; or (2) Indirect via carryover effect—a considerable time lag exists between the display of an advertisement and sales of the advertised product. In other words, a certain amount of sales generated by an advertisement is not achieved immediately after the expenditure and deployment of the advertisement. Previous research has reported empirical evidence of carryover effect in online advertising channels. For example, Johnson et al. [31] analyzed 432 online display advertising field experiments on the Google Display Network, and found most campaigns have a modest and positive carryover. Previous research has recognized the necessity of considering carryover effect of SEA, as demonstrated in a formal analysis by Archak et al. [32]. However, empirical evidence on carryover effect on actual sale volume generated by SEA is still lacking.

Besides the expenditure, other well-recognized factors for SEA success include ad positions and consumer behaviors over ads. In SEA, ad position is a key factor that advertisers compete for as higher ad positions are expected to generate more traffics and sales [33,34]. Therefore, higher ad positions are usually given to higher bidders if competing ads have the same relevance and quality.

While advertisers care about how many times their ads are displayed to consumers, how consumers interact with their ads is more important. Thus, major search engines predominantly adopt the pay-per-click scheme and charge an advertiser only when their ads are clicked by consumers. The PPC scheme has three important measures of consumer behaviors: Click-through-rate is the ratio of clicks on an ad over impressions by consumers. Conversion rate is the ratio of conversions (e.g., making a purchase) over the total number of ad clicks. In fact, many previous studies have used both measures as proxies to quantify the performance of SEA campaigns [33,35]. The third measure, cost-per-click, is directly related to the relationship between the expenditure and outcomes, because it is an advertiser’s expenditure on an ad divided by the number of clicks generated from the ad. For an advertiser, the actual CPC serves as a measure of how efficiently the advertising expenditure are generating clicks [36].

Researchers have also investigated relationships between ad positions and consumer behavior measures [37]. Most studies agreed that CPC and CTR monotonically decrease when ad positions are lower [33,37,34]. However, inconsistent findings exist for CVR. On one hand,
some [37,34] agreed that CVR is higher for ads at higher positions and decreases for lower ad positions. On the other hand, Agarwal et al. [33] noticed that CVR could increase with lower ad positions. The reason is that, while ad positions do affect CTR, after a consumer clicks an ad, whether a conversion will occur depends mainly on the website and the product, instead of the ad position in the SERP [34].

Given the strong connection between ad positions and consumer behaviors, researchers have attempted to help advertisers place ads in the right positions. For example, Ghose and Yang [37] revealed that for search engines, bidding prices are more important than prior CTR for the final position of an advertisement. Keywords with more prominent positions are not necessarily the more profitable ones for advertisers. Jeziorski and Moorthy [38] also studied the substitutional relationship between ad positions and advertisers’ brand strength, and suggested that advertisers with strong brands do not necessarily need to bid for the highest position. Recently, Zhuang et al. [39] investigated the role of that advertisers with strong brands do not necessarily need to bid for the highest position. Recently, Zhuang et al. [39] investigated the role of price information in consumers’ responses (e.g., clicks and conversions) to product list advertising, and revealed that consumers tend to click on the highest or lowest priced options in the early phases of the purchase funnel, while in later phases, they are more likely to click on moderately priced options.

Due to the highly dynamic nature of SEA, many studies have also modelled dynamic advertising processes and related decisions. One such decision is as bidding for keywords using different strategies at different funnel, while in later phases, they are more likely to click on moderately priced options.

From the methodological perspective, our study is related to time-varying modeling [17,43]. When dealing with longitudinal data, researchers often want to explicitly capture changes in the association between covariates and the outcome over time in a flexible manner. Thus Tan et al. [43] introduced a time-varying coefficient (TVC) model—a special case of varying-coefficient model [44]. It has been used to explore the changing roles of regulatory regimes, marketing mailers, transaction characteristics and demographic factors on international trades and marketing outcomes [45,46,47].

Specifically, the TVC model has three characteristics that fit this study. First, it is capable of estimating time-varying effects of covariates on the dependent variable. Thus TVC models are a generalized form of traditional linear regression models by incorporating time as the third dimension and representing coefficients of covariates with smoothly time-varying functions. Second, compared to multi-level (or hierarchical) modeling (MLM) frameworks that can also capture temporal associations between time-varying covariates and the outcome, a TVC model is more flexible and could effectively reveal any arbitrary “data-driven” shapes of covariates’ time-varying effects on the outcome, as long as coefficient functions are smooth (i.e., with no sudden jumps or break points). In addition, in the TVC model framework, researchers can also specify a certain functional form when they have sufficient prior knowledge and evidence, while allowing others to change freely. By contrast, an MLM has to assume a specific form of coefficient functions (e.g., linear, quadratic, or cubic) for trajectory shapes. Admittedly, estimating a TVC model needs more data than a parametric model does [43]. Third, a TVC model can handle the co-existence of multiple covariates in the same model, including time-varying ones along with time-invariant ones.

Overall, our research is distinct from the extant SEA research in the following ways. First, we propose a time-varying response model for SEA and estimate its parameters using a large-scale dataset from a major e-commerce retailer. Compared to advertising models in the literature, our model incorporates a quality-adjustment structure and is more appropriate for the dynamic context of SEA. Therefore, our approach also reveals several key findings that have not been found by or even contradict previous studies.

\footnote{A function is smooth if its first-order derivative function is continuous.}

Second, we are the first study to systematically investigate roles of a comprehensive set of factors, including the advertising expenditure, carryover effect, consumer behaviors (e.g., CTR and CVR), and advertisement-specific characteristics (e.g., ad position) and keyword-specific characteristics (e.g., the length of keywords, and appearances of retailers, brands and holidays), in generating sales from SEA. More importantly, we study these factors’ dynamic roles from a longitudinal perspective, so that we can reveal how their effects on sales change over time during an extended period of SEA campaigns.

Third, this is one of the few studies focusing directly on sales generated from SEA campaigns and studies the ad-sales relationship. Compared to marketing outcome measures based on consumers’ clicks, the focus on sales can more accurately and directly quantify advertisers’ financial gains from SEA campaigns and better inform their decision-making and planning in such campaigns.

3. Data and variables

This research uses a large-scale panel dataset collected from SEA campaigns by a large U.S. retailer, which offers a wide range of consumer electronics such as home appliances, air purifiers, etc. The retailer owns a large nationwide retail chain with brick-and-mortar stores and an electronic commerce website. The company has continuously conducted SEA campaigns over several years, and recorded data about SEA advertisements and online sales generated by these ads. The dataset we use is about SEA campaigns by this retailer during a 33-month period, spanning 4 calendar years from September 2005 to June 2008. The dataset is valid because the search advertising schema remains (almost) unchanged in the past decade. Moreover, the dataset contains almost 7 million time-stamped records from nearly 40,000 key search phrases and almost 55,000 advertisements, which is quite rich to support our empirical study.

Each record in the dataset is about one advertisement on a given day. Specifically, a record includes keywords that triggered the ad, the number of impressions, the number of clicks, the average CPC, the number of conversions (i.e., purchase or orders), the total number of items ordered, and generated sales. Note that the search query of a keyword may lead to an impression (i.e., display) of a related ad, but not necessarily a click; a click may not lead to a conversion (i.e., an order), and an order may include one or more items. We believe this dataset is appropriate for investigating the time-varying ad-sales relationship in SEA, because sales from SEA are available and the dataset covers a long time period that is sufficient to estimate a time-varying model [43]. There are few empirical studies of SEA using a dataset that has such a large scale, covers such a long time span, or contains such a rich range of advertising and keyword attributes.

Because this paper focuses on the ad-sales relationship, we directly use the number of products (in units) sold online (Sales) from each advertisement during a day as the dependent variable. There are several key independent variables whose effects on sales are of interests of Table 1 provides a list of all variables, along with their summary statistics, in this research. Table 2 illustrates the pairwise correlation among these variables.

The first one is the expenditure (AdExpenditure) spent on an SEA advertisement on a given day. We also include three independent variables for consumer’s click behaviors–CTR, CVR, and CPC–and one independent variable for advertisement characteristics–ad position. At the first glance, it may seem that the transitive relationship from impressions, through clicks to conversions is simply linear in SEA. In other words, the number of clicks on an ad is the product of the number of impressions and CTR. Similarly, the number of conversions is the product of the number of clicks and CVR. However, such linear relationships do not necessarily hold, because CTR and CVR are not constants. Also, the relationship between the advertising expenditure and the number of clicks is essentially nonlinear because cost-per-click (CPC) also changes over time. Thus, we investigate the dynamic influence of
score mainly considers three factors: exact formulas to calculate quality scores vary from one search engine to another, search engines have widely adopted quality scores for ads, such scores can lead to more clicks and potentially higher sales. However, while the advertiser can pay less for each click, so the same advertising budget improves revenue \[49, 50\]. For advertisers, a higher-quality ad means an ad ranking mechanism that considers advertising quality facilitates significant influence on the ad placement. \[4\]

Computed correlation used Pearson-method with listwise-deletion.

Table 1: A Summary of variables.

<table>
<thead>
<tr>
<th>Variables</th>
<th>Description</th>
<th>Mean</th>
<th>Std. Dev.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sales(Sales)</td>
<td>The total amount of sales (in units)</td>
<td>16.271</td>
<td>3521.487</td>
</tr>
<tr>
<td>Lagged Sales(Lagged Sales)</td>
<td>Sales from the previous time step (in units)</td>
<td>16.271</td>
<td>3521.487</td>
</tr>
<tr>
<td>Advertising Expenditure</td>
<td>Total spending (in dollars) during a day</td>
<td>149.842</td>
<td>2160.421</td>
</tr>
<tr>
<td>Ranking Position</td>
<td>The ranking position of an ad on the SERP</td>
<td>7.894</td>
<td>10.922</td>
</tr>
<tr>
<td>Cost-Per-Click(CPC)</td>
<td>The cost-per-click of an ad</td>
<td>18.245</td>
<td>53.637</td>
</tr>
<tr>
<td>Click-Through-Rate(CTR)</td>
<td>The click-through-rate of an ad</td>
<td>0.040</td>
<td>0.131</td>
</tr>
<tr>
<td>Conversion Rate (CVR)</td>
<td>The conversion-rate of an ad</td>
<td>0.003</td>
<td>0.045</td>
</tr>
<tr>
<td>Length of Keywords (KLength)</td>
<td>The number of words in a keyword for an ad</td>
<td>2.622</td>
<td>0.803</td>
</tr>
<tr>
<td>Brand(Retailer)</td>
<td>Binary variable-if associated keywords contain one or more specific brand names</td>
<td>0.175</td>
<td>0.380</td>
</tr>
<tr>
<td>Retailer(Holiday)</td>
<td>Binary variable-if associated keywords contain one or more specific retailer names</td>
<td>0.028</td>
<td>0.167</td>
</tr>
<tr>
<td>Holiday(Holiday)</td>
<td>Binary variable-if associated keywords contain one or more specific holiday names</td>
<td>0.003</td>
<td>0.054</td>
</tr>
</tbody>
</table>

Table 2: Pairwise correlation coefficients among variables.

<table>
<thead>
<tr>
<th>Sales</th>
<th>Saleslag1</th>
<th>Expenditure</th>
<th>Position</th>
<th>CTR</th>
<th>CPC</th>
<th>CVR</th>
<th>KLength</th>
<th>Retailer</th>
<th>Brand</th>
<th>Holiday</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sales</td>
<td>1</td>
<td>0.954***</td>
<td>0.135***</td>
<td>0.003***</td>
<td>0.026***</td>
<td>0.000</td>
<td>0.007***</td>
<td>0.028***</td>
<td>0.028***</td>
<td>0.000</td>
</tr>
<tr>
<td>Saleslag1</td>
<td>0.135***</td>
<td>1</td>
<td>0.134***</td>
<td>0.003***</td>
<td>0.015***</td>
<td>0.000</td>
<td>0.023***</td>
<td>0.004***</td>
<td>0.009***</td>
<td>0.000</td>
</tr>
<tr>
<td>Expenditure</td>
<td>0.003***</td>
<td>0.0135***</td>
<td>1</td>
<td>0.000</td>
<td>0.000</td>
<td>0.186***</td>
<td>0.032***</td>
<td>0.084***</td>
<td>0.080***</td>
<td>1</td>
</tr>
<tr>
<td>Position</td>
<td>0.003***</td>
<td>0.000</td>
<td>0.196***</td>
<td>1</td>
<td>0.125***</td>
<td>0.015***</td>
<td>0.168***</td>
<td>0.023***</td>
<td>0.009***</td>
<td>1</td>
</tr>
<tr>
<td>CTR</td>
<td>0.026***</td>
<td>0.000</td>
<td>0.000</td>
<td>1</td>
<td>0.015***</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
</tr>
<tr>
<td>CPC</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>1</td>
<td>0.221***</td>
<td>0.221***</td>
<td>0.000</td>
<td>0.000</td>
<td>1</td>
</tr>
<tr>
<td>CVR</td>
<td>0.007***</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>1</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
</tr>
<tr>
<td>KLength</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>1</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
</tr>
<tr>
<td>Retailer</td>
<td>0.007***</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>1</td>
<td>0.000</td>
<td>0.000</td>
</tr>
<tr>
<td>Brand</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>1</td>
<td>0.000</td>
</tr>
<tr>
<td>Holiday</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>1</td>
</tr>
</tbody>
</table>

4. Model development

Our model, defined in Eq. (1), has one dependent variable \(y_{ij}\), the sales from subject \(i\) at the \(j\)-th observation for advertising performance (i.e., sales from ads) along with a set of independent and control variables \(x_{ijk}\):

\[
y_{ij} = \beta_0(t_0) + \sum_{k=1}^{K} \beta_k(t_k)x_{ijk} + \epsilon_{ij},
\]

\[i = 1, \ldots, N; j = 1, \ldots, M; k = 1, \ldots, K.\]

In Eq. 1, \(N\) represents the total number of subjects (i.e., an advertisement), \(M\) is the total number of measurements (of features) for subject \(i\), and \(K\) is the number of explanatory variables; \(t_j\) is the measurement time of the \(j\) – th observation for the \(i\) – th subject. \(\beta_0(t_0)\) and \(\beta_k(t_k)\) are the coefficient functions to be estimated: the intercept \(\beta_0(t_0)\) represents the mean of \(y\) when \(x_k = 0\) at time \(t_0\). The slope, \(\beta_k(t_k)\), represents the strength and direction of the influence of \(x_k\) on \(y\) at time \(t_j\). Note that \(\beta_0(t_0)\) and \(\beta_k(t_k)\) are continuous coefficient functions of time \(t\), such that their values change over time. Random errors \(\epsilon_{ij}\) in the above equation are assumed to be normally and independently distributed. Although time-varying parameters are treated as non-parametric functions, the class of TVC models is parametric for a specified time \(t\). Thus the TVC model can be considered as conditionally parametric.

2 https://support.google.com/adwords/answer/6167118
3 https://www.wordstream.com/blog/ws/2012/06/04/quality-score-landing-pages-faq
4 https://support.google.com/adwords/answer/2404196
5 Note that data can be unbalanced with different assessment time within and across individual subjects.
representing a semi-parametric approach [47].

### 4.1. A time-varying SEA response model

With the nonlinear and temporal ad-sales relationship in SEA [33,37,34], we present an advertising response model for SEA in the TVC modeling framework (shown in Fig. 1). It does not assume any function forms for temporal trajectories of covariate coefficients. We also incorporate a quality-adjusted structure [53,54] to account for latent effects of advertising quality on ad performance.

#### 4.1.1. The basic model

The basic model adopts the advertising response model by Arnold et al. [55]. The model is an advertising spending function adjusted by a quality index based on the hedonic price theory (HPT) [56]. Because the outcome of a given amount of advertising spending depends on quality of the advertising copy, HPT can be naturally adopted to model the latent effects of advertising quality on ad performance. As discussed earlier in this paper, the quality of an ad explicitly affects the relationship between the advertising expenditure and sales, and needs to be controlled in our model. Therefore, following the Arnold model, we present a time-varying quality-adjusted response model for SEA below:

\[
\text{Sales}_{ij} = e^{\alpha(t_j)} \cdot (\psi_{ij})^{\beta(t_j)} \cdot D_{ij} \cdot e^{\varepsilon_{ij}}, \tag{2}
\]

where \(\text{Sales}_{ij}\) represents the number of products sold from advertisement \(i\) at time \(t_j\); \(\psi_{ij}\) is the advertising expenditure adjusted by the quality of advertisement \(i\) measured at time \(t_j\). Note that advertising quality is latent and we will discuss how to estimate the quality-adjusted advertising spending function in the next subsection. \(D_{ij}\) represents other covariates for sales. Details of them are in Subsection 4.1.3. In addition, \(\varepsilon_{ij}\) is the normally distributed error term at time \(t_j\); \(\alpha(t_j)\), the intercept coefficient, and \(\beta(t_j)\) will be estimated.

#### 4.1.2. The HPT-based advertising spending function

Following the quality-adjusted market price in classical HPT [56], we specify the quality-adjusted advertising expenditure function \(\psi_{ij}\) from Eq. (2) as below:

\[
\psi_{ij} = \left( B_{ij} \prod_{k=1}^{K} q_{ik} \right) \rho(t_j), \tag{3}
\]

where \(B_{ij}\) denotes the advertising spending (measured in dollar) at time \(t_j\); \(q_{ik}(k = 1, \ldots, K)\) is the value of advertisement attribute \(k\) that determines an ad’s quality score; \(\prod_{k=1}^{K} q_{ik}\) is thus the multi-dimensional quality index that is equivalent to the quality adjustment factor in [54](p.85), which adjusts the impact of the actual spending \((B)\) based on the advertising quality.

Specifically, in our case, as discussed in Section 3, five attributes of an ad could affect its quality score: CTR, the length of keywords, and time-invariant \(x_{ij}\), which represents the joint effects of four characteristics of keywords associated with advertisement \(i\): \(K\text{Length}_{ij}\), \(Retailer_{ij}\), \(Brand_{ij}\), and \(Holiday_{ij}\). Five coefficient functions \(r_1(t_j), r_2(t_j), r_3(t_j), r_4(t_j),\) and \(r_5(t_j)\) will be estimated.

#### 4.1.3. Ad position, CVR and CPC

In addition to the expenditure, CTR, and keyword characteristics, three more independent variables—ad position, CVR, and CPC—are included in \(D_{ij}\), which is defined in Eq. (5), where \(\text{Positions}_{ij}\) is the position of advertisement \(i\) on SERPs, \(\text{CPC}_{ij}\) and \(\text{CVR}_{ij}\) are the cost-per-click and conversion rate of advertisement \(i\), respectively, measured at time \(t_j\); \(\lambda_1(t_j), \lambda_2(t_j), \lambda_3(t_j)\) and \(\lambda_4(t_j)\) are the parameters to be estimated.

\[
D_{ij} = \prod_{m=1}^{M} \prod_{n=1}^{N} e^{x_{ij}^{m,n} \cdot e^{\varepsilon_{ij}}} = e^{(\text{Positions}_{ij})^{1(t_j)} \cdot \text{CPC}_{ij}^{2(t_j)} \cdot \text{CVR}_{ij}^{3(t_j)} \cdot (\text{CTR}_{ij})^{4(t_j)}}, \tag{5}
\]

#### 4.1.4. The SEA response model

Substituting Eqs. (4) and (5) into Eq. (2), we get Eq. (6). After taking natural logarithm transformations on numeric variables in Eq. (6), we obtain Eq. (7).

![Diagram](image.png)

**Fig. 1.** The conceptual structure of the time-varying SEA response model.
control function approach, which has been widely used to eliminate the error term of Eq. (8). To account for such endogeneity, we use the advertising budget and one or more unobserved latent factors in the carryover parameter in the Koyck model, the carryover parameter in the partial adjustment framework characterizes the complete dynamic nature of the advertising response [19]. Then Eq. (7) is transformed into Eq. (8):

\[
\ln Sales_{it} = \eta(t_i)a_0(t_i) + (1 - \eta(t_i))\ln Sales_{i,t-1} + \eta(t_i)\ln AdExpenditure_{it} + \tau_1(t_i)\ln CTR_{it} + \tau_2(t_i)KLength_{it} + \tau_3(t_i)Retailer_{it} + \tau_4(t_i)Brand_{it} + \tau_5(t_i)Holiday_{it} + \lambda_1(t_i)AdPosition_{it} + \lambda_2(t_i)\ln CPC_{it} + \lambda_3(t_i)\ln CVR_{it} + \varepsilon_{it},
\]

(8)

where \(\eta(t_i)\) is the partial adjustment coefficient, and \((1 - \eta(t_i))\) denotes the carryover effect at time \(t_i\). As \(\eta(t_i) \rightarrow 1\), the effect of advertising on sales is mainly instantaneous and the carryover effect hardly exists; conversely, as \(\eta(t_i) \rightarrow 0\), sales become increasingly persistent.

4.1.6. Accounting for the endogeneity of budgeting policies

In general, advertisers need to allocate their expenditures over advertisements strategically to achieve marketing objectives (e.g., maximizing revenues from SEA campaigns) [8,61]. Such budgeting policies could lead to the endogeneity problem [62]; the estimated effect of advertising budget on sales might be biased by the correlation between advertising budget and one or more unobserved latent factors in the error term of Eq. (8). To account for such endogeneity, we use the control function approach, which has been widely used to eliminate the endogeneity bias with marketing mix variables in marketing research [63,64].

\[
\ln Sales_{it} = \phi_w^B + \mu_{it}^B + \zeta_1(t_i)\ln Demand_{it} + \zeta_2(t_i)\ln CPC_{it} + \varepsilon_{it},
\]

(9)

where \(\varepsilon_{it}^B\) indicates the vector of exogenous variables (i.e., \(Demand_{it}\), \(CTR_{it}\), and \(CPC_{it}\)) for the advertising expenditure, \(\phi_w^B\) is the unknown parameter vector, and the random error \(\mu_{it}^B\) is assumed to be independently and normally distributed.

In the second stage, we include estimated residual \(\tilde{\mu}_{it}^B\) as an addi-
Table 3

<table>
<thead>
<tr>
<th>Coefficients</th>
<th>Dependent Variables</th>
</tr>
</thead>
<tbody>
<tr>
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<td>CPC</td>
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<td>CTR</td>
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<td>AIC</td>
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*** p < .001.

Table 4

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<tr>
<th>Model specifications</th>
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<th>BIC</th>
</tr>
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<td>−4,226,431</td>
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<tr>
<td>MODEL-Time-Varying-cubic</td>
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<td>−4,300,328</td>
<td>−4,299,688</td>
<td>−4,295,353</td>
</tr>
</tbody>
</table>

5.1. Budget endogeneity correction

Table 3 presents the first stage results of our control function approach (i.e., Eq. 9), which corrects the potential endogeneity from strategic budget allocation policies. Results confirm advertisers’ strategic budgeting decisions in SEA campaigns. Specifically, three exogenous variables—search demand, CPC and CTR—are all positive and statistically significant predictors for the advertising expenditure.

Theoretically, in the PPC scheme, the influence of search demand, CPC and CTR on the advertising expenditure should be similar and close to 1.0, because the expenditure can be computed as the product of these three factors. However, in our results, CPC appears to be the most influential factor for the advertising expenditure, followed by CTR and search demand. In other words, advertisers tend to emphasize on CPC and pay the least attention to search demand. This phenomenon is in line with the principles of information obtainability and least effort in information seeking behaviors [67]. On one hand, the principle of information obtainability states that, information that is more accessible to people is the more likely to be used by people, and vice versa. Similarly, according to the principle of least effort, when solving problems, a person tends to minimize her effort (over time). In the case of SEA, CPC has the highest obtainability for advertisers among the three factors, which is the most intuitive for them to understand and improve. This is because, for keywords with higher CPC (and bid prices), advertisers have to invest more in order to get sufficient opportunities to be displayed on SERPs and then clicked by search users.

By contrast, although advertisers often realize CTR’s importance and have strong motivations to improve it, it takes much more time and effort to achieve a higher CTR and predict its temporal changes [36]. Also, precise information about search demand is challenging for advertisers to obtain during their campaigns. Even though some search engines or third-party companies (e.g., WordTracker) provide potential information about search demand in a certain market, it is generally difficult for ordinary advertisers to predict the future search demand on daily basis and adjust advertising policies accordingly in a real-time way.

5.2. Model fit comparisons

Instead of a specific knot selection process, P-Spline-based approaches only need a large enough knot number (see Appendix for details), yet there is no agreement on the optimal number of knots (K). Wand [68] suggested the lower number between 35 and T/4, where T denotes the number of distinctive measurement times. Ruppert [69] recommended that K around 10 is enough to estimate monotonic functions and K around 20 is needed for complicated functions. Our dataset is unbalanced with different assessment time points within and across individual ads (i.e., 1 ≤ T ≤ 958). In order to estimate parameters of our SEA response model (Eqs. 9 and 10), we start with the B-Spline-based approach to fine-tune the analysis by incrementally increasing or decreasing the number of knots, and eventually use K = 30 in the P-Spline-based approach to estimate our model. We choose P-Splines over B-Splines because P-Splines can produce smoother estimates of the coefficient functions.

Next, we evaluate our time-varying model in terms of model fit by comparing it with several alternative specifications. The first alternative is a time-invariant model (MODEL-Time-Invariant), which treats coefficients of covariates in our full model (i.e., Eqs. 9 and 10) as time-invariant constants. We also compare three variants of our time-varying model fit statistics of the proposed model and alternative specifications.
varying model specified with linear (MODEL-Time-Varying-linear), quadratic (MODEL-Time-Varying-quadratic) and cubic (MODEL-Time-Varying-cubic) spline functions, respectively. Table 4 illustrates model fit statistics for these various specifications, including twice the negative of the residual log likelihood (–2 Res Log Likelihood), the Akaike information criterion (AIC) and the Bayesian information criterion (BIC).

As Table 4 shows, our time-varying advertising model specified with cubic splines provides the best fit, followed by MODEL-Time-Varying-quadratic and MODEL-Time-Varying-linear, while MODEL-Time-Invariant has the worst fit. In other words, including temporal dynamics helps time-varying models significantly improve their model fit compared to the time-invariant model. Theoretically, time-varying models break the study period into more fine-grained time intervals (rather than treat it as a single interval) and can reveal much more information about relationships between the explanatory variables and the dependent variable [43]. Also, the best fit by cubic spline function, compared to the linear and quadratic functions, highlights the dynamic complexity of SEA markets [70].

To examine the effect of each covariate on sales, we also analyze estimated parameters from our time-invariant model with budget endogeneity correction (i.e., treating coefficients of Eqs. 9 and 10 as constants) because such coefficients are easier to be understood and interpreted than coefficient functions. Results in Table 5 reveal two interesting findings: First, the budget correction term ($\mu_{ij}$) has a statistically significant effect ($\alpha_1 = 0.069, p < 0.001$), which justifies the addition of budget control function (i.e., Eq. 9) to the model. Second, compared to other covariates, the budget correction term explains a substantial part of the variance in the dependent variable (Sales). This suggests that, there are indeed some unobserved factors associated with advertisers’ budgeting decisions. The positive effect of the budget correction term also implies that, without the budget correction process, parameter estimates of the advertising expenditure will be biased upwards, because the original model (in Eq. 8) omits unobserved factors that correlate with the advertising expenditure.

### 5.2.1. Carryover effect

From Table 5, we can see that the variable for lagged sales ($Sales_{t-1}$) has a statistically significant and positive effect on sales ($\gamma^* = 0.695, p < 0.001$). Also, the coefficient of lagged sales fluctuates between 0.648 and 0.774 over time (Fig. 2). Similar to traditional advertising, lagged sales remain a significant predictor for current sales in the context of SEA. This is in line with what has been reported in the literature [71,72,73]. The carryover effect is also higher in SEA than those reported in traditional advertising channels (e.g., via newspapers, radio, TV, and billboards) [55,29,74]. Although Dinner et al. [65] argued that the

---

**Table 5**

Estimated parameters for the time-invariant model with budget endogeneity correction.

<table>
<thead>
<tr>
<th>Coefficients</th>
<th>Dependent Variables</th>
</tr>
</thead>
<tbody>
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<td>Sales</td>
<td>Estimates</td>
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<td>(Intercept)</td>
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<td>Log Sales</td>
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<td>Ad Expenditure</td>
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<tr>
<td>Ad Position</td>
<td>0.000***</td>
</tr>
<tr>
<td>CTR</td>
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</tr>
<tr>
<td>CVR</td>
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</tr>
<tr>
<td>Keyword Length</td>
<td>-0.007***</td>
</tr>
<tr>
<td>Brand</td>
<td>0.002***</td>
</tr>
<tr>
<td>Retailer</td>
<td>0.053***</td>
</tr>
<tr>
<td>Holiday</td>
<td>-0.001</td>
</tr>
<tr>
<td>B-Residuals</td>
<td>0.069***</td>
</tr>
<tr>
<td>Observations</td>
<td>5,649,220</td>
</tr>
<tr>
<td>R²/adj. R²</td>
<td>0.693 / 0.693</td>
</tr>
</tbody>
</table>

*** p < .001.
Fig. 3. Estimated coefficient functions of ad-specific factors (Straight lines represent linear curve fitting).
carryover effect is almost zero in SEA, their study was based on one apparel retailer, whose main revenue (nearly 85%) is generated through offline channels. However, in the e-commerce dataset we use, all sales driven by SEA are fulfilled online, which makes the estimation of carryover effect less biased. From a temporal perspective, the carryover effect is persistent and strong in SEA over time. In general, the carryover effect has an upward trend in SEA, as shown in Fig. 2. In addition, the trend is not monotonic in SEA, highlighting the complex dynamics in carryover effect.

5.2.2. The ad-sales relationship

The coefficient of independent variable AdExpenditure represents the short-term advertising elasticity. According to Table 5, the advertising expenditure has a statistically significant and positive effect on sales ($\beta^s = 0.001, p < 0.001$). The coefficient of the advertising expenditure fluctuates between 0.001 and 0.007 over time (Fig. 2). It drops first before increases and fits a linear line with a positive slope.

Overall, despite the statistical significance, the magnitude of the current advertising expenditure’s effect on sales is small. This contradicts the commonly-held views in traditional advertising that the advertising expenditure is the major driving force to generate direct-response sales [29,30]. One possible reason for the difference is that millions of competing advertisers in SEA lead to more intense competitions [75,76] and thus lower advertising elasticity [65,30].

5.2.3. Ad positions, CTR and CVR

In this section, we investigate effects of advertisement characteristics (i.e., ad position) and consumer behavior measures (i.e., CTR and CVR) on sales (see Fig. 3).

Ad position is a statistically significant predictor of sales, but has a low coefficient ($\lambda^p_{1} = 0.0001397$ and $p < 0.001$). In other words, if an ad’s position goes up by one unit, the contemporary sales is expected to increase by only 0.014%. According to Fig. 3, the effect of ad positions drops very fast over time. We also estimate a model with an additional quadratic term of ad position on ads listed on the first search engine results page (SERP). However, the new model still has close to zero coefficients for both ad position and its quadratic term. We will discuss the implications of this finding later in this paper.

Click-through rate (CTR) is a statistically significant and positive predictor of sales ($\lambda^c_{1} = 0.035, p < 0.001$). Such a low coefficient is not surprising, because click-through is primarily a consequence of the brand building in online advertising. Moreover, Fig. 3 shows that the influence of CTR on sales declines over the promotion period. Its effect on sales even becomes negative at the final stage of the campaigns move on, that is, ads with a lower CTR can produce more sales than those with a higher CTR. This is probably because at the later stage of a SEA campaign, certain search users get to know the advertiser and their ads better, and consider the advertiser’s SEA ads as a quality source for products they desire. Consequently, when they do click an ad from the advertiser, they tend to purchase a higher amount of products [77].

Conversion rate (CVR) is a statistically significant predictor of sales, with a stronger effect on sales ($\lambda^c_{2} = 2.392, p < 0.001$) than CTR. Meanwhile, CVR’s influence on sales fluctuates over time.

5.2.4. Control variables

To represent latent advertising quality, we add control variables (Fig. 4) to the model. Keywords length negatively influences sales ($\lambda^k_{1} = -0.007, p < 0.001$) – a longer and more specific keyword leads to fewer sales than shorter and more general keywords. Even though consumers who search for more general keywords usually have lower CVR, a more general keyword can trigger much more clicks, leading to more sales. As for what is in a keyword, containing a brand and containing a retailer in an ad are positive predictors of sales while containing a holiday is not. Also, all control variables’ coefficient functions trend downward over time.

5.3. Accounting for unobservable factors at the individual level

To account for unobservable factors at the individual level, we ran a separate panel model with fixed effects. Even though the model does not provide time-varying coefficients, it would serve as a good robustness check for results from our TVC framework. Note that, in our model, $i$ refers to the index of subjects (i.e., advertisements) and $j$ refers to the index of observations. In other words, for different advertisements, the same $j$ may correspond to different time of observations. For example, one ad was observed during the period from Jan. 1 to Jan. 10, while another ad was observed during the period of from Jan. 3 to Jan. 15. For example, $j = 1$ would correspond to Jan. 1 for the former ad and Jan. 3 for the latter ad. Hence, adding fixed effects on $j$ makes little sense. Therefore, we estimate fixed-effects and random-effects models on advertisements (i.e., $i$) and conducted the Hausman test to choose between the two models. The results reveal that the Hausman test statistic is significant with $p < 0.001$, suggesting that the fixed-effects model is an appropriate choice for our research. Results of the panel model with fixed effects on advertisements (Table 6) are consistent with the time-invariant model and the TVC model.

5.4. Accounting for heteroscedasticity and nonindependence among observations

To account for heteroscedasticity and nonindependence among observations, we cluster standard errors by advertisements for the panel model with fixed effects. Our dataset is organized by each advertisement on a daily basis and our model (Eq. 10) is estimated at the individual advertisement level. While it makes little sense to cluster errors at the level of $j$, in order to further check the results of our model, we cluster the standard errors at the level $i$ to account for heteroscedasticity and nonindependence among observations across days for each advertisement. Table 7 presents the estimated coefficients of the fixed effects model and robust standard errors clustered by advertisement. The results show that the estimated coefficients remain consistent, while robust standard errors clustered by advertisement become larger, compared to those of the fixed effects model.

6. Conclusions

6.1. Theoretical implications

Our research has theoretical implications to the research of SEA. First, this study contributes to the SEA literature by taking into account the temporal variations in the effectiveness of various types of SEA factors and addressing an important gap in the literature. SEA is one of the most dynamic advertising environments with interactive behaviors between users and advertisers, auction processes and mechanisms. This research contributes to our understanding of dynamics in SEA. Although previous research (e.g., [33,37,34]) reported non-linear effects of ad advertising variables, our research is the first to reveal the time-varying pattern of these effects. Moreover, our model implicitly encapsulates the concept of advertising quality score as a latent variable by adopting a quality-adjustment structure. This allows us to explore influence trajectories of advertising expenditure and various related factors on the expected market outcome (i.e., sales) over time. In addition, our results reveal non-linear pattern in the temporal effects of various key factors in SEA on sales. This finding can inform future studies of temporal dynamics in SEA.

Second, this study adds to the broader line of research on advertising response models by capturing the dynamic ad-sales relationship in the SEA context. Conceptually, different advertising forms may be described by different ad-response models distinct by the underlying mechanisms and inherent advertising variables. Although prior research has adapted the Vidale-Wolfe model [28] to the SEA context for the purpose of supporting optimal budget allocation, their model fails to incorporate
Fig. 4. Estimated coefficient functions of control variables (Straight lines represent linear curve fitting).
more advertising variables except for a quality score index, due to the limitation of differential-equation modeling structure. Our response model not only incorporates rich advertising features of SEA, but also is capable of handling the time-varying effects of various factors.

Moreover, our research empirically compares short-term advertising elasticity and carryover effect on SEA sales based on a large-scale dataset from a major U.S. e-commerce retailer. Results show that the carryover effect is stronger than the short-term elasticity and suggest that SEA is not a direct-response advertising medium. Instead, advertisers need to be patient and make a longer-term advertising investment before getting returns in sales. This also calls for more research on long-term strategies for SEA including budget allocation, bid pricing and keywords selections, because ordinary advertisers have little knowledge and time to operate such sophisticated and dynamical campaigns in the long run.

Third, our research also finds important patterns on how advertisers make budget decisions in SEA. We find that SEA advertisers mainly consider CPC, instead of CTR and search demand, when making such decisions. More explorations on advertisers’ behaviors in different advertising schemes can help search engines improve their market design.

Last, our research helps to better understand the inefficiency in the current SEA scheme. Prior studies [33,37] have found that higher positions on SERPs are not necessarily the more profitable ones for advertisers. Our research finds one potential reason for this. Advertising performance evaluation based on CTR is inevitably biased, because SEA campaigns experience a significant, positive and increasing carryover effect. In addition, the effects of CVR and CTR on sales make it possible to design a hybrid advertising scheme that combines pay-per-click and pay-per-action.

6.2. Practical implications

This research provides several practical implications for SEA advertisers. First, our findings could serve as the basis for designing a decision-support tool that helps advertisers better understand the ad-sales relationships, especially the influence of various factors on sales, and how their influences change over time. More importantly, the tool based on our model enables advertisers to predict advertising performance and allocate their advertising resources accordingly in a real-time fashion for their SEA campaigns. For instance, our time-varying response model can be used to generate close-loop budget strategies over time via developing an optimal control model of budget planning (e.g., [8]). However, budget optimization is beyond the scope of this research.

Second, for advertisers, focusing only on the direct and immediate effect of the expenditure on sales would underestimate the performance of their SEA campaigns in terms of sales, because SEA features a significant carryover effect that is more influential than the immediate effect. In other words, the effect of the advertising expenditure on sales would be overestimated without considering lagged sales (Table 5). In practice, given the temporal dynamics in the carryover effect in SEA, advertisers could consider increasing/decreasing their advertising budget when the coefficient of the carryover effect is on the rise/decline, in order to get bigger “bang of the buck”.

Third, our research also reveals the effects of advertisement characteristics and consumer behavior measures on SEA sales. For instance, advertisers may want to carefully evaluate the return on investment of bidding for higher ad positions on SERPs. Our finding offers empirical evidence that always bidding for higher ad positions may lead to limited increase in sales and possibly hurt return on investment. Different from search engines’ traditional stance, our results could offer alternative advertising strategies.

Among measures of consumers behaviors, besides CTR, SEA advertisers should also pay extra attention to CVR, because it is directly associated with sales. Moreover, it is more important for an advertiser to improve its CVR during the initial stage of its SEA campaigns, because the influence of CVR gradually declines over time.

Last but not the least, advertisers can adjust keyword selection strategies over time—they can focus on shorter and more general keywords in the initial stage of a campaign, and then increase the portion of longer and more specific keywords over time. It also helps to improve sales if an advertiser can include more retailer-specific and brand-specific keywords during the initial stage of a campaign.

6.3. Limitations and future research

We acknowledge several limitations of our research. First, similar to most, if not all, studies using advertising response models, we investigate the ad-sales relationship in SEA at the campaign level, rather than consumer behaviors at the individual level. The former is about how to allocate resources on advertising campaigns, while the latter focuses on how an advertiser should bid for a keyword in an auction against rivals. Our focus on the former means that our model cannot discern the heterogeneity inherent in behaviors of individual advertisers and their competitors.

Second, our study is limited by the dataset we used. For example, the dependent variable in our study is sales measured by the units of practice, given the temporal dynamics in the carryover effect in SEA, our model entitles advertisers to predict advertising performance and systematically understand the temporal pattern of each factor on sales, and how their influences change over time. More importantly, the tool based on our model enables advertisers to predict advertising performance and allocate their advertising resources accordingly in a real-time fashion for their SEA campaigns. For instance, our time-varying response model can be used to generate close-loop budget strategies over time via developing an optimal control model of budget planning (e.g., [8]). However, budget optimization is beyond the scope of this research.

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Second, our study is limited by the dataset we used. For example, the dependent variable in our study is sales measured by the units of products sold from SEA campaigns. Sales is certainly important for advertisers and is often considered more valuable than clicks [1]. However, return on investment is often more important in business [78], because it combines the advertising expenditure and the profit from transactions, and can be a more straightforward way to measure an advertisers’ financial gains. Besides monetary outcomes, some advertisers may also value the positive image of their brand gained from SEA campaigns. At the same time, even though our dataset is large in scale and covers an extended period of time, whether our conclusions apply to SEA in other contexts needs further investigations.

This research can be extended in several ways. One direction is to systematically understand the temporal pattern of each factor on sales, so that dynamic strategies for optimal resource allocation can be designed. Based on such a time-varying advertising response model, the

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**Table 6**

Results of the panel model with fixed effects on advertisements.

<table>
<thead>
<tr>
<th>Coefficients</th>
<th>Dependent Variables</th>
</tr>
</thead>
<tbody>
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</tr>
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</tr>
<tr>
<td>CTR</td>
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<tr>
<td>CVR</td>
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<tr>
<td>B-Residuals</td>
<td>0.064 ***</td>
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<tr>
<td>Observations</td>
<td>5,649,220</td>
</tr>
<tr>
<td>R²/adj. R²</td>
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</tr>
</tbody>
</table>

***p < .001.

**Table 7**

Results of the panel model with fixed effects and robust standard errors clustered by advertisements.

<table>
<thead>
<tr>
<th>Coefficients</th>
<th>Dependent Variables</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Sales</td>
</tr>
<tr>
<td>Estimates</td>
<td>Conf. Int.</td>
</tr>
<tr>
<td>Lagged Sales</td>
<td>0.396 ***</td>
</tr>
<tr>
<td>Ad Expenditure</td>
<td>0.002 ***</td>
</tr>
<tr>
<td>Ranking Position</td>
<td>-0.000 ***</td>
</tr>
<tr>
<td>CTR</td>
<td>0.024 ***</td>
</tr>
<tr>
<td>CVR</td>
<td>2.404 ***</td>
</tr>
<tr>
<td>B-Residuals</td>
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</tr>
<tr>
<td>Observations</td>
<td>5,649,220</td>
</tr>
<tr>
<td>R²/adj. R²</td>
<td>0.39053 / 0.38534</td>
</tr>
</tbody>
</table>

***p < .001.
discrete-time optimal control technology can be utilized to get a close-loop solution for resources allocation for SEA campaigns. Then formal field experiments can be designed and executed to improve model fits and support advertising resource allocation in real time. Second, it will be interesting to adopt the panel vector autoregression (PVAR) model to explore dynamic inter-dependency between a set of advertising factors in the SEA context, which could significantly enhance our understanding of the underlying mechanism currently adopted by major search engines. In particular, the PVAR analysis can also be supplemented with generalized forecast error variance decomposition to shed light on the relative power of each advertising variable and impulse response function to visualize the dynamical relationship between each pair of variables. Third, we plan to extend our model to include the continual bidding process and advertisers’ behaviors at the individual level. In addition, time-varying interactions between advertisers and consumers should be an interesting topic to explore in the field of SEA as well.

CRediT authorship contribution statement

Yanwu Yang: Conceptualization, Methodology, Investigation,

Appendix A

A.1. Estimation of the Time-varying search advertising response model

In the following we provide the estimation of the time-varying search advertising response model described in Section 4.1. P-splines have several very attractive merits. First, they do not impose any assumption on the changing pattern of a given explanatory variable with respect to time \( t \) (e.g., linear, quadratic, or cubic), which makes the estimated model immune to the misspecification problem [43]. Second, compared to smoothing approaches (e.g., regression splines, B-splines), P-splines have no boundary effects, can conserve moments of data and have polynomial fits as limits, and their computation are relatively inexpensive [66]. Accordingly, P-splines have been widely used in marketing literature on semi-parametric models (e.g., Stremersch and Lemmens [47], Saboo et al. [46]).

The general idea behind splines-based smoothers is that any smoothly varying (coefficient) function (e.g., \( f(t) \)) defined on a certain interval can be approximated by a linear combination of lower order polynomial base functions. Specifically, the interval is partitioned into small enough \( \tau \)-intervals for P-splines [43]. However, the number of knots is less crucial in P-splines based estimation approaches (e.g., 10, which also depends on the number of distinctive measurement times) for P-splines [43].

As an example, the coefficient function \( a(t_\tau) \) can be approximately represented as

\[
a(t_\tau) = a_0 + a_1 t_\tau + a_2 t_\tau^2 + \sum_{k=1}^{K} a_{q+k}(t_\tau - t_k)^q.
\]

By substituting a set of coefficient functions of \( t \) into the original model to be estimated, we can get a linear regression model with these base functions (such as 1, \( t_\tau, t_\tau^2, ..., (t_\tau - t_k)^q \)) as covariates and \( a_0, a_1, a_2, ..., a_{q+k} \) as coefficients, which can be easily estimated with ordinary least square (OLS). P-splines combine B-splines with different penalties on estimated coefficients, i.e., using “a simple difference penalty on the coefficients themselves of adjacent B-splines” [66], in order to address the overfitting problem. The approach suggested by Ruppert [69] and Wand [68] shrinks the coefficients of coefficient functions (e.g., \( a_{q+k}, k = 1, 2, ..., K \) in Eq. 10) towards zero, by minimizing the sum of S\( \text{SSE} \) (sum of squared errors) and the penalty term (defined as the summation of a series of products of coefficients and corresponding tuning parameters), i.e., \( \text{SSE} + \lambda \sum_{k=1}^{K} a_{q+k}(t_\tau - t_k)^q \) \( + \ldots \). The resulting optimal tuning terms (e.g., \( \lambda \)) balance the tradeoff between the goodness of fit and the smooth of the estimated functions. Thus, the penalty term could prevent these coefficients from being too large in absolute value. Wand [68] developed an approach that treats these coefficients as random variable with normal distribution, and expands the model to be estimated into a linear mixed-effect model, which can be estimated with the restricted maximum likelihood (REML) to the optimal balance. For more details on the P-splines estimation of non- and semi-parametric models, see [66,69,68].

Data availability

The authors do not have permission to share data.

Acknowledgements

We are thankful to the associate editor and anonymous reviewers who provided valuable suggestions that led to a considerable improvement in the organization and presentation of this manuscript. This work is partially supported by the (NSFC National Natural Science Foundation of China) grants (72171093, 71672067).


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